

Electrical Theory Two

26105-05



Alamo Data Center

Built in Fort Lauderdale, Florida, the Alamo Data Center project was unique because it required stringent clean-room procedures while the electrical work was being done. This was to protect the integrity of the facility and equipment used. Food and drink were prohibited, special uniforms were required, and the electricians were not even allowed to chew gum.

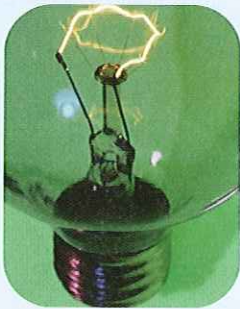
26105-05

Electrical Theory Two

Topics to be presented in this module include:

1.0.0	Introduction5.2
2.0.0	Resistive Circuits5.2
3.0.0	Kirchhoff's Laws5.10

Overview



Troubleshooting complex electrical or electronic circuitry requires an advanced understanding of electrical theory. When a complex circuit does not respond as designed, the electrician or technician must safely locate, determine, and repair the problem. To accomplish this task in a relatively short period and with reasonable success, the electrician must apply both fundamental concepts, such as Ohm's law, and more advanced concepts, such as Kirchhoff's laws. Studying advanced electrical theory is the only way to know when and where to apply such laws.

Objectives

When you have completed this module, you will be able to do the following:

1. Explain the basic characteristics of a series circuit.
2. Explain the basic characteristics of a parallel circuit.
3. Explain the basic characteristics of a series-parallel circuit.
4. Calculate, using Kirchhoff's voltage law, the voltage drop in series, parallel, and series-parallel circuits.
5. Calculate, using Kirchhoff's current law, the total current in parallel and series-parallel circuits.
6. Find the total amount of resistance in a series circuit.
7. Find the total amount of resistance in a parallel circuit.
8. Find the total amount of resistance in a series-parallel circuit.

Trade Terms

Kirchhoff's current law	Series circuits
Kirchhoff's voltage law	Series-parallel circuits
Parallel circuits	

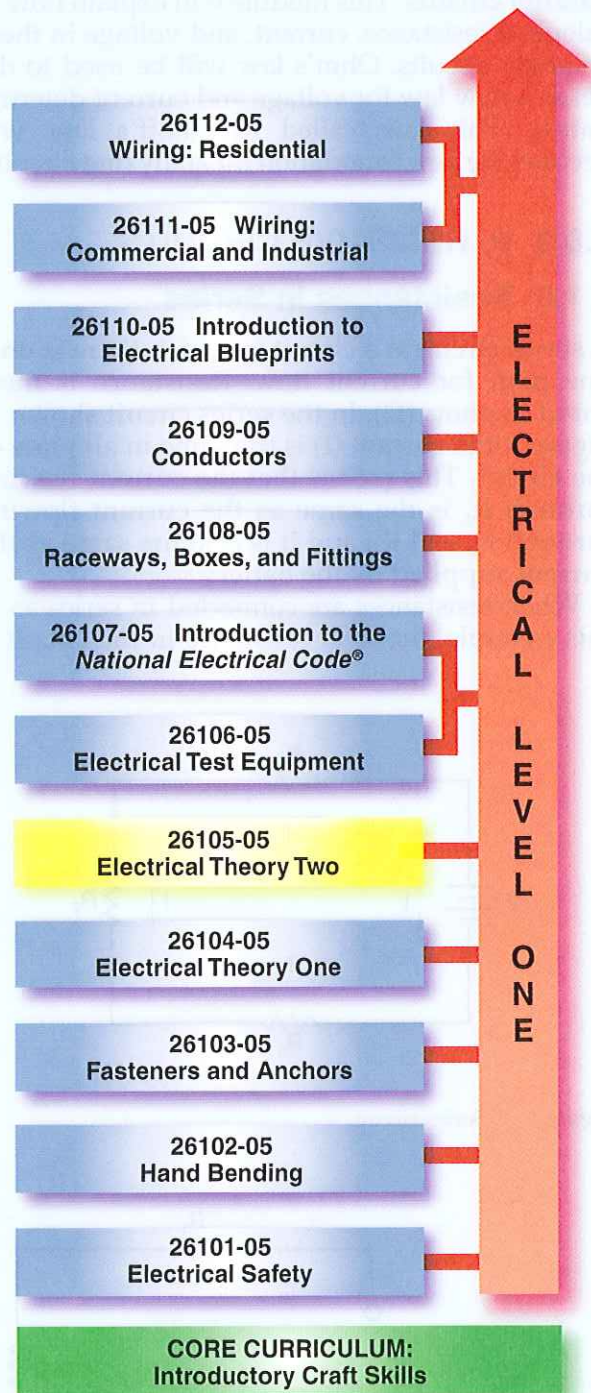
Required Trainee Materials

1. Paper and pencil
2. Appropriate personal protective equipment

Prerequisites

Before you begin this module, it is recommended that you successfully complete *Core Curriculum* and *Electrical Level One*, Modules 26101-05 through 26104-05.

This course map shows all of the modules in *Electrical Level One*. The suggested training order begins at the bottom and proceeds up. Skill levels increase as you advance on the course map. The local Training Program Sponsor may adjust the training order.



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1.0.0 ♦ INTRODUCTION

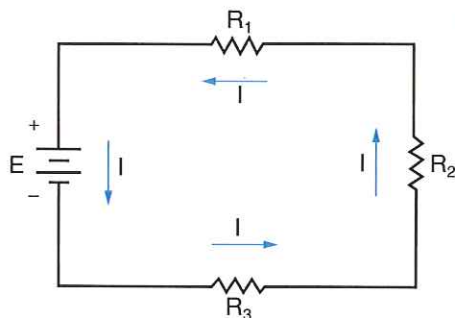
Ohm's law was explained in the module *Electrical Theory One*. This fundamental concept is now going to be used to analyze more complex **series circuits**, **parallel circuits**, and combination **series-parallel circuits**. This module will explain how to calculate resistance, current, and voltage in these complex circuits. Ohm's law will be used to develop a new law for voltage and current determination. This law, called Kirchoff's law, will become the new foundation for analyzing circuits.

2.0.0 ♦ RESISTIVE CIRCUITS

2.1.0 Resistances in Series

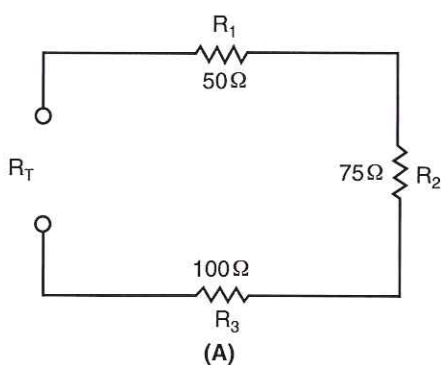
A series circuit is a circuit in which there is only one path for current flow. Resistance is measured in ohms (Ω). In the series circuit shown in *Figure 1*, the current (I) is the same in all parts of the circuit. This means that the current flowing through R_1 is the same as the current flowing through R_2 and R_3 , and it is also the same as the current supplied by the battery.

When resistances are connected in series as in this example, the total resistance in the circuit is

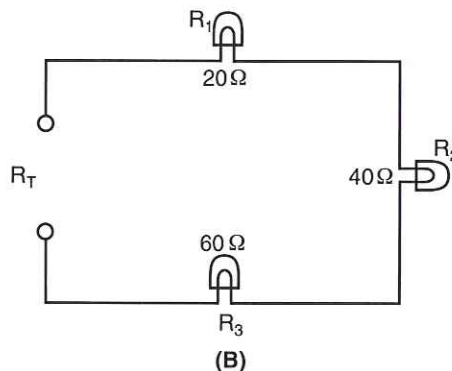


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Figure 1 ♦ Series circuit.



(A)



(B)

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Figure 2 ♦ Total resistance.

equal to the sum of the resistances of all the parts of the circuit:

$$R_T = R_1 + R_2 + R_3$$

Where:

R_T = total resistance

$R_1 + R_2 + R_3$ = resistances in series

Example 1:

The circuit shown in *Figure 2(A)* has 50Ω , 75Ω , and 100Ω resistors in series. Find the total resistance of the circuit.

Add the values of the three resistors in series:

$$R_T = R_1 + R_2 + R_3 = 50 + 75 + 100 = 225\Omega$$

Example 2:

The circuit shown in *Figure 2(B)* has three lamps connected in series with the resistances shown. Find the total resistance of the circuit.

Add the values of the three lamp resistances in series:

$$R_T = R_1 + R_2 + R_3 = 20 + 40 + 60 = 120\Omega$$

2.2.0 Resistances in Parallel

The total resistance in a parallel resistive circuit is given by the formula:

$$R_T = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_n}}$$

Where:

R_T = total resistance in parallel

$R_1, R_2, R_3,$ and R_n = branch resistances

Example 1:

Find the total resistance of the 2Ω , 4Ω , and 8Ω resistors in parallel shown in *Figure 3*.

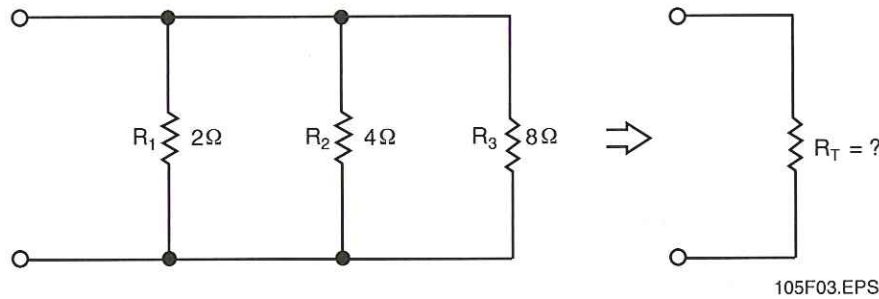



Figure 3 ♦ Parallel branch.



Series Circuits

Simple series circuits are seldom encountered in practical wiring. The only simple series circuit you may recognize is older strands of Christmas lights, in which the entire string went dead when one lamp burned out. Think about what the actual wiring of a series circuit would look like in household receptacles. How would the circuit physically be wired? What kind of illumination would you get if you wired your household receptacles in series and plugged half a dozen lamps into those receptacles?

Write the formula for the three resistances in parallel:

$$R_T = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

Substitute the resistance values:

$$R_T = \frac{1}{\frac{1}{2} + \frac{1}{4} + \frac{1}{8}}$$

$$R_T = \frac{1}{0.5 + 0.25 + 0.125}$$

$$R_T = \frac{1}{0.875}$$

$$R_T = 1.14\Omega$$

Note that when resistances are connected in parallel, the total resistance is always less than the resistance of any single branch.

In this case:

$$R_T = 1.14\Omega < R_1 = 2\Omega, R_2 = 4\Omega, \text{ and } R_3 = 8\Omega$$

Example 2:

Add a fourth parallel resistor of 2Ω to the circuit in Figure 3. What is the new total resistance, and what is the net effect of adding another resistance in parallel?

Write the formula for four resistances in parallel:

$$R_T = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}}$$

Substitute values:

$$R_T = \frac{1}{\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{2}}$$

$$R_T = \frac{1}{0.5 + 0.25 + 0.125 + 0.5}$$

$$R_T = \frac{1}{1.375}$$

$$R_T = 0.73\Omega$$

The net effect of adding another resistance in parallel is a reduction of the total resistance from 1.14Ω to 0.73Ω .

2.2.1 Simplified Formulas

The total resistance of *equal* resistors in parallel is equal to the resistance of one resistor divided by the number of resistors:

$$R_T = \frac{R}{N}$$

Where:

R_T = total resistance of equal resistors in parallel

R = resistance of one of the equal resistors

N = number of equal resistors

If two resistors with the same resistance are connected in parallel, the equivalent resistance is half of that value, as shown in *Figure 4*.

The two 200Ω resistors in parallel are the equivalent of one 100Ω resistor; the two 100Ω resistors are the equivalent of one 50Ω resistor; and the two 50Ω resistors are the equivalent of one 25Ω resistor.

When any two unequal resistors are in parallel, it is often easier to calculate the total resistance by multiplying the two resistances and then dividing the product by the sum of the resistances:

$$R_T = \frac{R_1 \times R_2}{R_1 + R_2}$$

Where:

R_T = total resistance of unequal resistors in parallel

R_1, R_2 = two unequal resistors in parallel

Example 1:

Find the total resistance of a 6Ω (R_1) resistor and an 18Ω (R_2) resistor in parallel:

$$R_T = \frac{R_1 \times R_2}{R_1 + R_2} = \frac{6 \times 18}{6 + 18} = \frac{108}{24} = 4.5\Omega$$

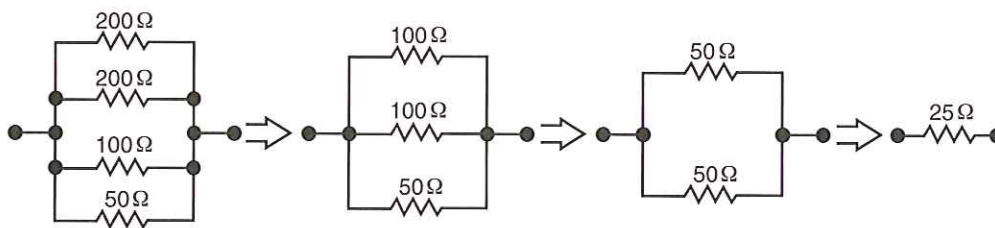


Figure 4 ♦ Equal resistances in a parallel circuit.

Example 2:

Find the total resistance of a 100Ω (R_1) resistor and a 150Ω (R_2) resistor in parallel:

$$R_T = \frac{R_1 \times R_2}{R_1 + R_2} = \frac{100 \times 150}{100 + 150} = \frac{15,000}{250} = 60\Omega$$

2.3.0 Series-Parallel Circuits

To find current, voltage, and resistance in series circuits and parallel circuits is fairly easy. When working with either type, use only the rules that apply to that type. In a series-parallel circuit, some parts of the circuit are series connected and other parts are parallel connected. Thus, in some parts the rules for series circuits apply, and in other parts, the rules for parallel circuits apply. To analyze or solve a problem involving a series-parallel circuit, it is necessary to recognize which parts of the circuit are series connected and which parts are parallel connected. This is obvious if the circuit is simple. Many times, however, the circuit must be redrawn, putting it into a form that is easier to recognize.

In a series circuit, the current is the same at all points. In a parallel circuit, there are one or more points where the current divides and flows in separate branches. In a series-parallel circuit, there are both separate branches and series loads. The easiest way to find out whether a circuit is a series, parallel, or series-parallel circuit is to start at the

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Parallel Circuits

An interesting fact about circuits is the drop in resistance in a parallel circuit as more resistors are added. But this fact does not mean that you can add an endless number of devices, such as lamps, in a parallel circuit. Why not?



Parallel Circuits

Most practical circuits are wired in parallel, like the pole lights shown here.



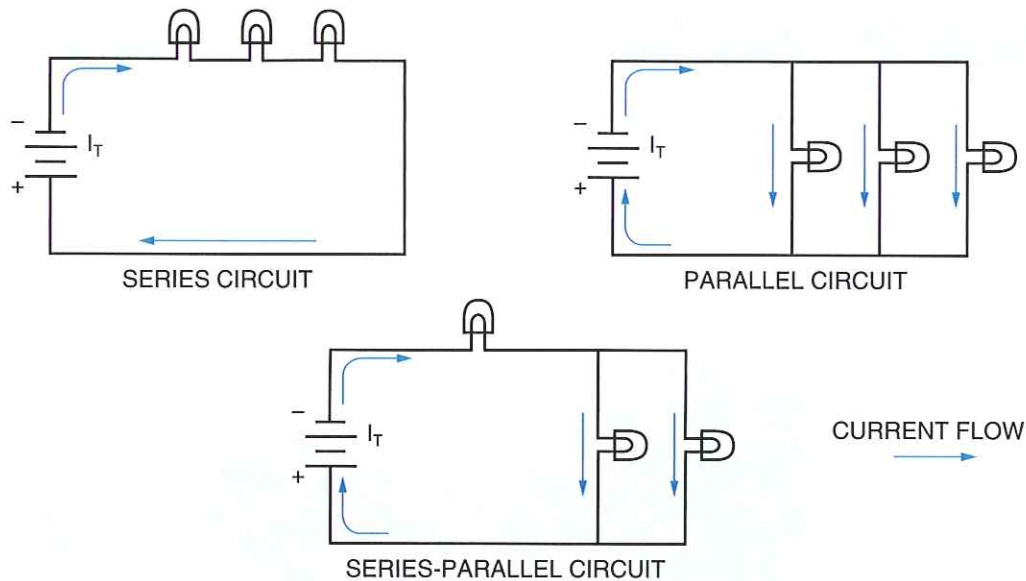
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negative terminal of the power source and trace the path of current through the circuit back to the positive terminal of the power source. If the current does not divide anywhere, it is a series circuit. If the current divides into separate branches, but there are no series loads, it is a parallel circuit. If the current divides into separate branches and there are also series loads, it is a series-parallel circuit. *Figure 5* shows electric lamps connected in series, parallel, and series-parallel circuits.

After determining that a circuit is series-parallel, redraw the circuit so that the branches and the series loads are more easily recognized. This is especially helpful when computing the total resistance of the circuit. *Figure 6* shows resistors connected in a series-parallel circuit and the equivalent circuit redrawn to simplify it.

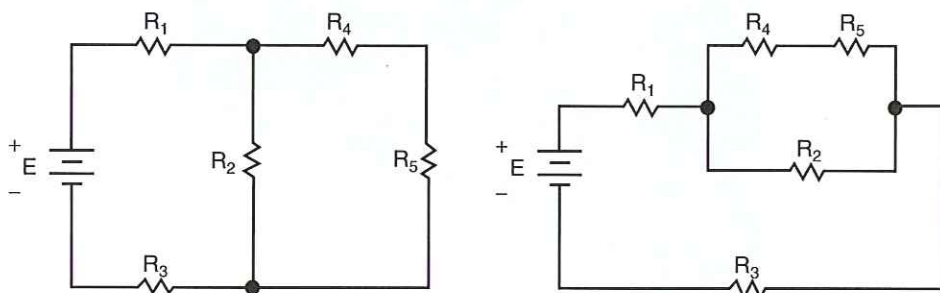
2.3.1 Reducing Series-Parallel Circuits

Very often, all that is known about a series-parallel circuit is the applied voltage and the values of the individual resistances. To find the voltage drop across any of the loads or the current in any of the branches, the total circuit current must usually be known. But to find the total current, the total resistance of the circuit must be known. To find the total resistance, reduce the circuit to its simplest form, which is usually one resistance that forms a series circuit with the voltage source. This simple series circuit has the equivalent resistance of the series-parallel circuit it was derived from, and also has the same total current. There are four basic steps in reducing a series-parallel circuit:




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Figure 5 ♦ Series, parallel, and series-parallel circuits.



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Figure 6 ♦ Redrawing a series-parallel circuit.



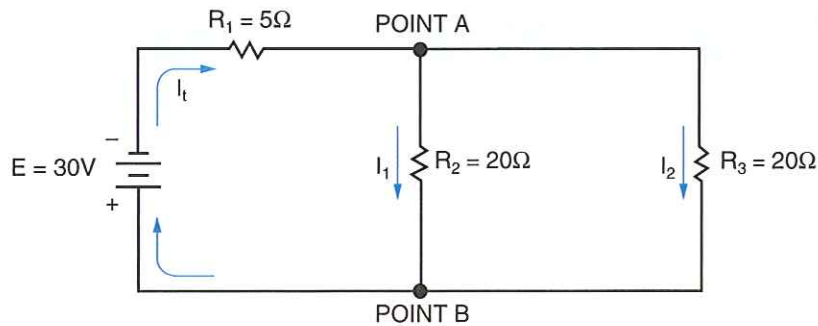
Series-Parallel Circuits

Explain Figure 6. Which resistors are in series and which are in parallel?

- If necessary, redraw the circuit so that all parallel combinations of resistances and series resistances are easily recognized.
- For each parallel combination of resistances, calculate its effective resistance.
- Replace each of the parallel combinations with one resistance whose value is equal to the effective resistance of that combination. This provides a circuit with all series loads.
- Find the total resistance of this circuit by adding the resistances of all the series loads.

Examine the series-parallel circuit shown in Figure 7 and reduce it to an equivalent series circuit.

In this circuit, resistors R_2 and R_3 are connected in parallel, but resistor R_1 is in series with both the battery and the parallel combination of R_2 and R_3 . The current I_T leaving the negative terminal of the voltage source travels through resistor R_1 before it is divided at the junction of resistors R_1 , R_2 , and R_3 (Point A) to go through the two branches formed by resistors R_2 and R_3 .



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Figure 7 ♦ Reducing a series-parallel circuit.

Given the information in *Figure 7*, calculate the resistance of R_2 and R_3 in parallel and the total resistance of the circuit, R_T .

The total resistance of the circuit is the sum of R_1 and the equivalent resistance of R_2 and R_3 in parallel. To find R_T , first find the resistance of R_2 and R_3 in parallel. Because the two resistances have the same value of 20Ω , the resulting equivalent resistance is 10Ω . Therefore, the total resistance (R_T) is 15Ω ($5\Omega + 10\Omega$).

2.4.0 Applying Ohm's Law

2.4.1 Voltage and Current in Series Circuits

In resistive circuits, unknown circuit parameters can be found by using Ohm's law and the techniques for determining equivalent resistance. Ohm's law may be applied to an entire series circuit or to the individual parts of the circuit. When it is used on a particular part of a circuit, the voltage across that part is equal to the current in that part multiplied by the resistance of that part.

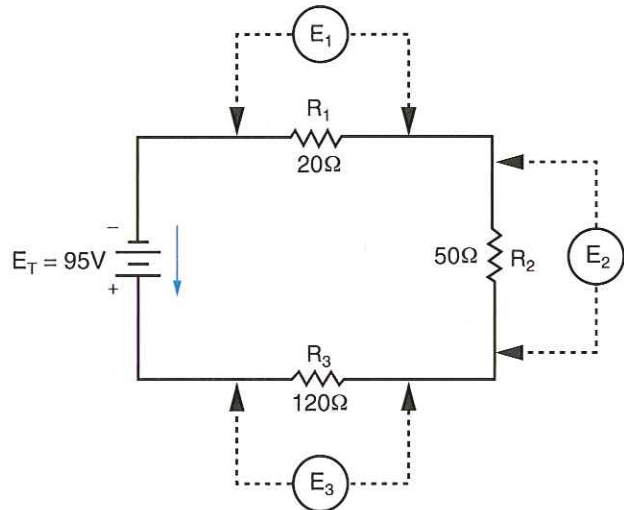
For example, given the information in *Figure 8*, calculate the total resistance (R_T) and the total current (I_T).

To find R_T :

$$\begin{aligned} R_T &= R_1 + R_2 + R_3 \\ R_T &= 20 + 50 + 120 \\ R_T &= 190\Omega \end{aligned}$$

To find I_T using Ohm's law:

$$\begin{aligned} I_T &= \frac{E_T}{R_T} \\ I_T &= \frac{95}{190} \\ I_T &= 0.5A \end{aligned}$$



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Figure 8 ♦ Calculating voltage drops.

Find the voltage across each resistor. In a series circuit, the current is the same; that is, $I = 0.5A$ through each resistor:

$$\begin{aligned} E_1 &= IR_1 = 0.5(20) = 10V \\ E_2 &= IR_2 = 0.5(50) = 25V \\ E_3 &= IR_3 = 0.5(120) = 60V \end{aligned}$$

The voltages E_1 , E_2 , and E_3 found for *Figure 8* are known as voltage drops or IR drops. Their effect is to reduce the voltage that is available to be applied across the rest of the components in the circuit. The sum of the voltage drops in any series circuit is always equal to the voltage that is applied to the circuit. The total voltage (E_T) is the same as the applied voltage and can be verified in this example ($E_T = 10 + 25 + 60$ or $95V$).

2.4.2 Voltage and Current in Parallel Circuits

A parallel circuit is a circuit in which two or more components are connected across the same



Voltage Drops

Calculating voltage drops is not just a schoolroom exercise. It is important to know the voltage drop when sizing circuit components. What would happen if you sized a component without accounting for a substantial voltage drop in the circuit?

voltage source, as illustrated in *Figure 9*. The resistors R_1 , R_2 , and R_3 are in parallel with each other and with the battery. Each parallel path is then a branch with its own individual current. When the total current I_T leaves the voltage source E , part I_1 of the current I_T will flow through R_1 , part I_2 will flow through R_2 , and the remainder I_3 will flow through R_3 . The branch currents I_1 , I_2 , and I_3 can be different. However, if a voltmeter is connected across R_1 , R_2 , and R_3 , the respective voltages E_1 , E_2 , and E_3 will be equal to the source voltage E .

The total current I_T is equal to the sum of all branch currents.

This formula applies for any number of parallel branches whether the resistances are equal or unequal.

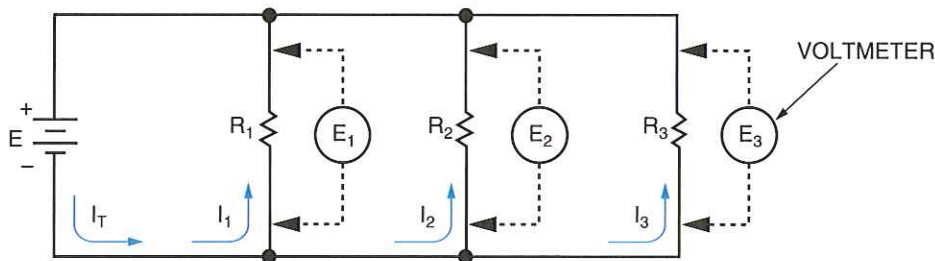
Using Ohm's law, each branch current equals the applied voltage divided by the resistance between the two points where the voltage is applied. Hence, for each branch in *Figure 9* we have the following equations:

$$\text{Branch 1: } I_1 = \frac{E_1}{R_1} = \frac{E}{R_1}$$

$$\text{Branch 2: } I_2 = \frac{E_2}{R_2} = \frac{E}{R_2}$$

$$\text{Branch 3: } I_3 = \frac{E_3}{R_3} = \frac{E}{R_3}$$

With the same applied voltage, any branch that has less resistance allows more current through it than a branch with higher resistance.



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Figure 9 ♦ Parallel circuit.

Example 1:

The two branches R_1 and R_2 , shown in *Figure 10(A)*, across a 110V power line draw a total line current of 20A. Branch R_1 takes 12A. What is the current I_2 in branch R_2 ?

Transpose to find I_2 and then substitute given values:

$$I_T = I_1 + I_2$$

$$I_2 = I_T - I_1$$

$$I_2 = 20 - 12 = 8A$$

Example 2:

As shown in *Figure 10(B)*, the two branches R_1 and R_2 across a 240V power line draw a total line current of 35A. Branch R_2 takes 20A. What is the current I_1 in branch R_1 ?

Transpose to find I_1 and then substitute given values:

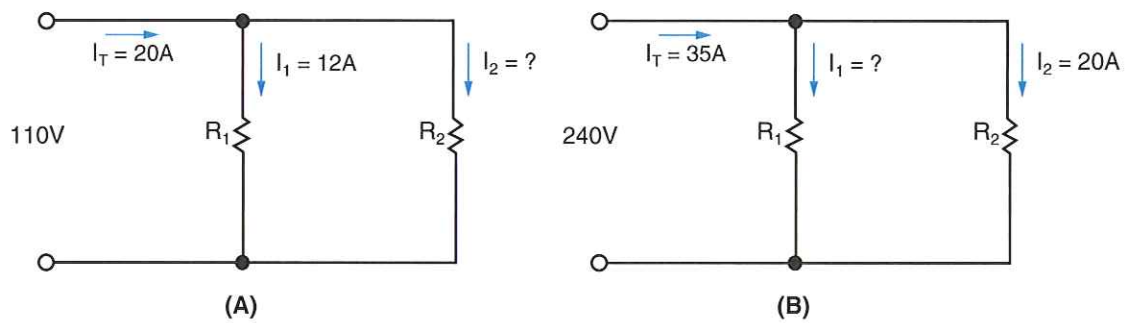
$$I_T = I_1 + I_2$$

$$I_1 = I_T - I_2$$

$$I_1 = 35 - 20 = 15A$$

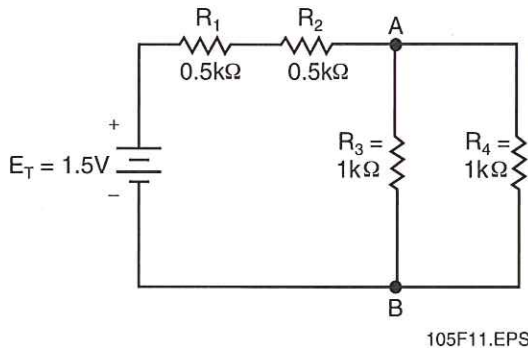
2.4.3 Voltage and Current in Series-Parallel Circuits

Series-parallel circuits combine the elements and characteristics of both the series and parallel configurations. By properly applying the equations and methods previously discussed, the values of individual components of the circuit can be determined. *Figure 11* shows a simple series-parallel circuit with a 1.5V battery.



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Figure 10 ♦ Solving for an unknown current.



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Figure 11 ♦ Series-parallel circuit.

The current and voltage associated with each component can be determined by first simplifying the circuit to find the total current, and then working across the individual components.

This circuit can be broken into two components: the series resistances R_1 and R_2 , and the parallel resistances R_3 and R_4 .

R_1 and R_2 can be added together to form the equivalent series resistance R_{1+2} :

$$\begin{aligned} R_{1+2} &= R_1 + R_2 \\ R_{1+2} &= 0.5\text{k}\Omega + 0.5\text{k}\Omega \\ R_{1+2} &= 1\text{k}\Omega \end{aligned}$$

R_3 and R_4 can be totaled using either the general reciprocal formula or, since there are two resistances in parallel, the product over sum method. Both methods are shown below.

$$\begin{aligned} R_{3+4} &= \frac{1}{\frac{1}{R_3} + \frac{1}{R_4}} = \frac{1}{\frac{1}{1\text{k}\Omega} + \frac{1}{1\text{k}\Omega}} \\ &= \frac{1}{\frac{2}{1,000\Omega}} = \frac{1}{0.002} = 500\Omega \end{aligned}$$

$$\begin{aligned} R_{3+4} &= \frac{R_3 \times R_4}{R_3 + R_4} = \frac{1\text{k}\Omega \times 1\text{k}\Omega}{1\text{k}\Omega + 1\text{k}\Omega} \\ &= \frac{1,000,000\Omega}{2,000\Omega} = 500\Omega \end{aligned}$$

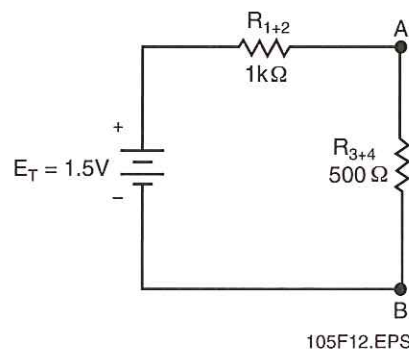
The equivalent circuit containing the R_{1+2} resistance of $1\text{k}\Omega$ and the R_{3+4} resistance of 500Ω is shown in Figure 12.

Using the Ohm's law relationship that total current equals voltage divided by circuit resistance, the circuit current can be determined. First, however, total circuit resistance must be found. Since the simplified circuit consists of two resistances in series, they are simply added together to obtain total resistance.

$$\begin{aligned} R_T &= R_{1+2} + R_{3+4} \\ R_T &= 1\text{k}\Omega + 500\Omega \\ R_T &= 1.5\text{k}\Omega \end{aligned}$$

Applying this to the current/voltage equation:

$$\begin{aligned} I_T &= \frac{E_T}{R_T} \\ I_T &= \frac{1.5\text{V}}{1.5\text{k}\Omega} \\ I_T &= 1\text{mA or } 0.001\text{A} \end{aligned}$$



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Figure 12 ♦ Simplified series-parallel circuit.

Now that the total current is known, voltage drops across individual components can be determined:

$$E_{R1} = I_T R_1 = 1\text{mA} \times 0.5\text{k}\Omega = 0.5\text{V}$$

$$E_{R2} = I_T R_2 = 1\text{mA} \times 0.5\text{k}\Omega = 0.5\text{V}$$

Since the total voltage equals the sum of all voltage drops, the voltage drop from A to B can be determined by subtraction:

$$E_T = E_{R1} + E_{R2} + E_{A+B}$$

$$E_T - E_{R1} - E_{R2} = E_{A+B}$$

$$1.5\text{V} - 0.5\text{V} - 0.5\text{V} = E_{A+B} = 0.5\text{V}$$

Since R_3 and R_4 are in parallel, some of the total current must pass through each resistor. R_3 and R_4 are equal, so the same current should flow through each branch. Using the relationship:

$$I = \frac{E}{R}$$

$$I_{R3} = \frac{E_{R3}}{R_3}$$

$$I_{R4} = \frac{E_{R4}}{R_4}$$

$$I_{R3} = \frac{0.5\text{V}}{1\text{k}\Omega}$$

$$I_{R4} = \frac{0.5\text{V}}{1\text{k}\Omega}$$

$$I_{R3} = 0.5\text{mA}$$

$$I_{R4} = 0.5\text{mA}$$

$$0.5\text{mA} + 0.5\text{mA} = 1\text{mA}$$

Therefore, the total current for the circuit passes through R_1 and R_2 and is evenly divided between R_3 and R_4 .

3.0.0 ◆ KIRCHHOFF'S LAWS

Kirchhoff's laws provide a simple, practical method of solving for unknown parameters in a circuit.

3.1.0 Kirchhoff's Current Law

In its most general form, **Kirchhoff's current law**, which is also called Kirchhoff's first law, states

that at any point in a circuit, the total current entering that point must equal the total current leaving that point. For parallel circuits, this implies that the current in a parallel circuit is equal to the sum of the currents in each branch.

When using Kirchhoff's laws to solve circuits, it is necessary to adopt conventions that determine the algebraic signs for current and voltage terms. A convenient system for current is to consider all current flowing into a branch point as positive, and all current directed away from that point as negative.

As an example, in *Figure 13*, the currents can be written as:

$$I_A + I_B - I_C = 0$$

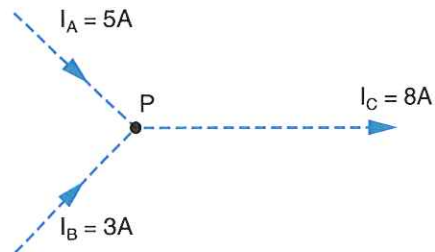
or

$$5\text{A} + 3\text{A} - 8\text{A} = 0$$

Currents I_A and I_B are positive terms because these currents flow into P, but I_C , directed out of P, is negative.

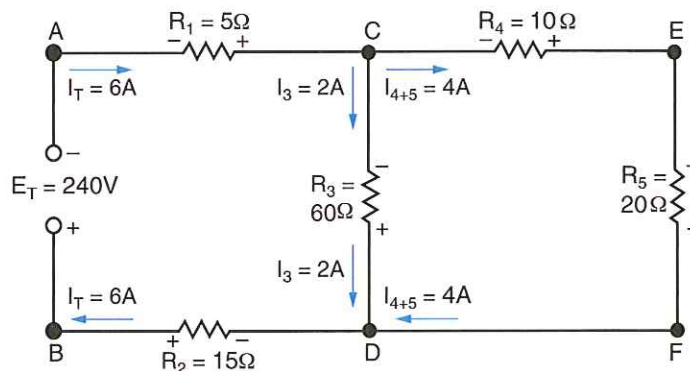
For a circuit application, refer to Point C at the top of the diagram in *Figure 14*. The 6A I_T into Point C divides into the 2A I_3 and 4A I_{4+5} , both directed out. Note that I_{4+5} is the current through R_4 and R_5 . The algebraic equation is:

$$I_T - I_3 - I_{4+5} = 0$$



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Figure 13 ◆ Kirchhoff's current law.



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Figure 14 ◆ Application of Kirchhoff's current law.

Substituting the values for each current:

$$6A - 2A - 4A = 0$$

For the opposite direction, refer to Point D at the bottom of *Figure 14*. Here, the branch currents into Point D combine to equal the mainline current I_T returning to the voltage source. Now, I_T is directed out from Point D, with I_3 and I_{4+5} directed in. The algebraic equation is:

$$I_3 + I_{4+5} - I_T = 0$$

$$2A + 4A - 6A = 0$$

Note that at either Point C or Point D, the sum of the 2A and 4A branch currents must equal the 6A total line current. Therefore, Kirchhoff's current law can also be stated as:

$$I_{IN} = I_{OUT}$$

For *Figure 14*, the equations for current can be written as shown below.

At Point C:

$$6A = 2A + 4A$$

At Point D:

$$2A + 4A = 6A$$

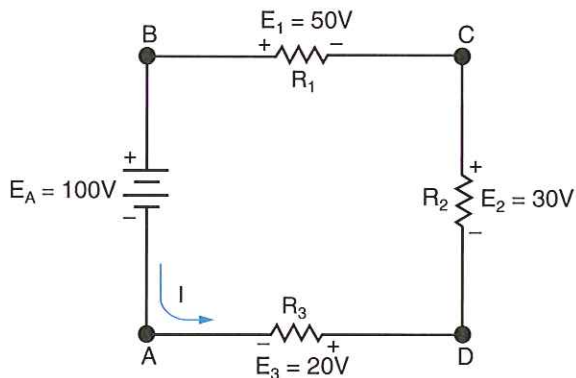
Kirchhoff's current law is really the basis for the practical rule in parallel circuits that the total line current must equal the sum of the branch currents.

3.2.0 Kirchhoff's Voltage Law

Kirchhoff's voltage law states that the algebraic sum of the voltages around any closed path is zero.

Referring to *Figure 15*, the sum of the voltage drops around the circuit must equal the voltage applied to the circuit:

$$E_A = E_1 + E_2 + E_3$$



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Figure 15 ♦ Kirchhoff's voltage law.

Where:

E_A = voltage applied to the circuit

$E_1, E_2,$ and E_3 = voltage drops in the circuit

Another way of stating this law is that the algebraic sum of the voltage rises and voltage drops must be equal to zero. A voltage source is considered a voltage rise; a voltage across a resistor is a voltage drop. (For convenience in labeling, letter subscripts are shown for voltage sources and numerical subscripts are used for voltage drops.) This form of the law can be written by transposing the right members to the left side:

$$\text{Voltage applied} - \text{sum of voltage drops} = 0$$

Substitute letters:

$$E_A - E_1 - E_2 - E_3 = 0$$

$$E_A - (E_1 + E_2 + E_3) = 0$$

3.3.0 Loop Equations

Any closed path is called a loop. A loop equation specifies the voltages around the loop. Refer to *Figure 16*.

Consider the inside loop A, C, D, B, A, including the voltage drops $E_1, E_3,$ and $E_2,$ and the source E_T . In a clockwise direction, starting at Point A, the algebraic sum of the voltages is:

$$- E_1 - E_3 - E_2 + E_T = 0$$

or

$$- 30V - 120V - 90V + 240V = 0$$

Voltages $E_1, E_3,$ and E_2 have a negative value, because there is a decrease in voltage seen across each of the resistors in a clockwise direction. However, the source E_T is a positive term because an increase in voltage is seen in that same direction.

For the opposite direction, going counterclockwise in the same loop from Point A, E_T is negative while $E_1, E_2,$ and E_3 have positive values. Therefore:

$$- E_T + E_2 + E_3 + E_1 = 0$$

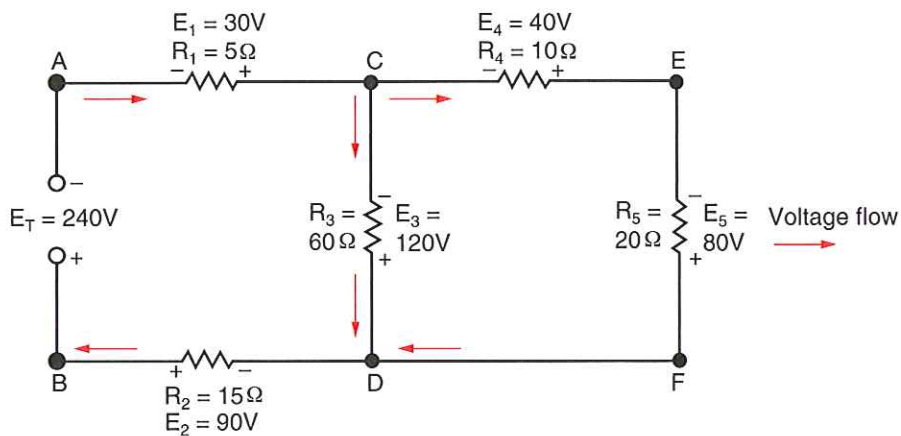
or

$$- 240V + 90V + 120V + 30V = 0$$

When the negative term is transposed, the equation becomes:


$$240V = 90V + 120V + 30V$$

In this form, the loop equation shows that Kirchhoff's voltage law is really the basis for the practical rule in series circuits that the sum of the voltage drops must equal the applied voltage.



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Figure 16 ♦ Loop equation.



Putting It All Together

Draw four 60W lamps in parallel with a 120V power source. What is the amperage in the circuit? What would happen to the amperage if we doubled the voltage?

For example, determine the voltage E_B for the circuit shown in *Figure 17*. The direction of the current flow is shown by the arrow. First mark the polarity of the voltage drops across the resistors and trace the circuit in the direction of the current flow starting at Point A. Then write the voltage equation around the circuit:

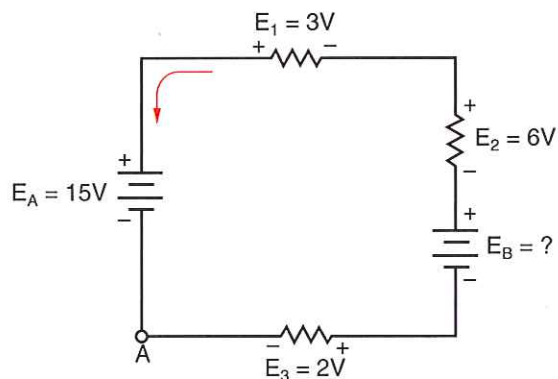
$$- E_3 - E_B - E_2 - E_1 + E_A = 0$$

Solve for E_B :

$$\begin{aligned} E_B &= E_A - E_3 - E_2 - E_1 \\ E_B &= 15V - 2V - 6V - 3V \\ E_B &= 4V \end{aligned}$$

Since E_B was found to be positive, the assumed direction of current is in fact the actual direction of current.

In its most general form, Kirchhoff's voltage law (also called Kirchhoff's second law) states that the algebraic sum of all the potential differences in a closed loop is equal to zero. A closed loop means any completely closed path consist-



105F17.EPS

Figure 17 ♦ Applying Kirchhoff's voltage law.

ing of wire, resistors, batteries, or other components. For series circuits, this implies that the sum of the voltage drops around the circuit is equal to the applied voltage. For parallel circuits, this implies that the voltage drops across all branches are equal.

The background of the page features several faint circuit diagrams. On the left, there is a bridge-like circuit with four diodes. On the right, there is a circuit with a resistor, a battery, and a lamp. At the top center, there is a simple series circuit with a battery, a resistor, and a lamp. The text 'Summary' is centered in a blue rounded rectangle.

Summary

The relationships among current, voltage, resistance, and power in Ohm's law are the same for both DC series and DC parallel circuits. Understanding and being able to apply these concepts is necessary for effective circuit analysis and troubleshooting. DC series-parallel circuits also have these fundamental relationships. Since DC series-parallel circuits are a combination of simple series

and parallel circuits, Kirchhoff's voltage and current laws will apply. Calculating I, E, R, and P for series-parallel circuits is no more difficult than calculating these values for simple series or parallel circuits. However, for series-parallel circuits, these calculations require more careful circuit analysis in order to use Ohm's law correctly.

Notes



James Mitchem

TIC—The Industrial Company

Jim Mitchem serves as a troubleshooter for a large electrical contractor. During his career in the electrical industry, he worked his way up from apprentice to technical services manager.

How did you become an electrician?

Quite by accident. A couple of years after college, I was working as a relief operator in a plant when the lead electrician retired, creating a vacancy. I liked the idea that electricians were expected to use their knowledge and initiative to keep the place running. I applied and was accepted as a trainee.

How did you get your training?

I took an electrical apprenticeship course by correspondence, and I was fortunate enough to work with good people who helped me along. I worked in an environment that exposed me to a variety of equipment and applications, and just about everyone I've ever worked with has taught me something. Now I'm passing my knowledge on to others.

What kinds of work have you done in your career?

I've worked as an apprentice, journeyman, instrument and controls technician, instrument fitter, foreman, general foreman, superintendent, and startup engineer. Each of these positions required that I learn new skills, both technical and managerial. My experience in many disciplines and types of projects has given me a high level of credibility with my employer and our clients.

Now I act as a technical resource and troubleshooter for job sites and in-house functions such as safety, quality assurance, and training. I visit job sites to help solve problems and help out with commissioning and startup.

What factor or factors have contributed the most to your success?

There are several factors. Two very important ones have been a desire to learn and a willingness to do whatever is asked of me. I also keep an eye on the big picture. When I'm on a job, I'm not just pulling wire, I'm building a power plant or whatever the project is. I also think it has helped me to remain with the same employer for 18 years.

Any advice for apprentices just beginning their careers?

Keep learning! And don't depend on others to train you. Take the initiative to buy or borrow books and trade journals. Take licensing tests and do whatever is necessary to keep your licenses current. Finally, make sure you know your own personal and professional values and work with a company that shares those values.

Trade Terms Introduced in This Module

Kirchhoff's current law: The statement that the total amount of current flowing through a parallel circuit is equal to the sum of the amounts of current flowing through each current path.

Kirchhoff's voltage law: The statement that the sum of all the voltage drops in a circuit is equal to the source voltage of the circuit.

Parallel circuits: Circuits containing two or more parallel paths through which current can flow.

Series circuits: Circuits with only one path for current flow.

Series-parallel circuits: Circuits that contain both series and parallel current paths.



Additional Resources

This module is intended to present thorough resources for task training. The following reference works are suggested for further study. These are optional materials for continued education rather than for task training.

Electronics Fundamentals: Circuits, Devices, and Applications, Thomas L. Floyd. New York: Prentice Hall.

Principles of Electric Circuits, Thomas L. Floyd. New York: Prentice Hall.

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